Mixture Models for Multi-Species and Environmental Data

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- Ecological inference and management decisions often depend on data from many species.
- A proper and useful statistical analysis quantifies the important patterns of variation, whilst reducing the complexity in multi-species data.
- Currently, analysis is frequently done by: 1) performing species-by-species analyses (e.g. univariate regression and extensions) and then combining results, or 2) by combining data (clustering) and then performing a group-by-group analysis.
- Neither of the standard approaches are entirely satisfactory as important aspects of the variance in the data can be lost when moving from step to step. Also, the propagation of uncertainty is difficult and is subsequently (often) ignored.
- We introduce two models, based on mixture models, that address these issues. One model type, species archetype models (SAMs) exploits similarities in individual species’ responses to the environment. The second type, regions of common profile (RCP) models, exploits similarities in the assemblage patterns at each site.

Models

We use 2 variants of mixture models to represent variation in data from many species. Let the species’ data be given by \((y_i)\) and the environmental data be \((x_i, x)\), where \(i = 1 ... N\) index sites and \(j = 1 ... S\) index species. We have used these methods for \(S = 300\) species and \(N = 1200\) - limited by size of survey data at the moment.

Species Archetype Models (SAMs, for when inference on species is required)

Mixture of regressions model to group individual species’ responses to environmental gradients into archetypal patterns. Only \(K \ll S\) archetypal responses are interpreted, instead of \(S\) models from a species-by-species analysis. The model for the expectation is:

\[
E[y_{ij}] = \sum_{k=1}^{K} \pi_k E[y_{ij} | \text{archetype } k], \quad \text{where}
\]

\[
y \left( E[y_{ij} | \text{archetype } k] \right) = \alpha_i + w_j' \tau_j + x_i' \beta_k
\]

and the distribution of each species’ data may have species-specific parameters \([1, 2, 3, 4, 5]\).

See Figure 1 for some archetypal environmental responses of fish off the south-east coast of mainland Australia. Analysis performed using physical environmental covariates, biomass data and a Tweedie model.

Regions of Common Profiles (RCP, for when inference on sites is required)

Mixture of experts model to group sites based on its species prole in relation to environment. This allows interpretation of only \(H \ll N\) RCPs to study assemblage-environment relationships. No species, nor site, is hard-clustered into a particular RCP. The model for expectation is:

\[
E[y_{ij}] = \sum_{k=1}^{H} \pi_h(w_i, x_j) E[y_{ij} | \text{RCP } h],
\]

where \(\pi_h(w_i, x_j)\) is a multinomial logit link function [6].

See Figure 2 for the predicted probability of each region-type, based on fish assemblages for the North West Shelf of Australia. Analysis performed using physical environmental covariates and fish presence/absence data.

Benefits of Using SAMs and RCPs

- Interpretability - complexity of multi-species data reduced by clustering species (SAMs) or sites (RCPs) [1, 6, 4].
- Prediction Performance - rarer species ‘borrow strength’ from common species [3].
- Diagnostics - checking model adequacy, e.g. residual plots [2, 5].
- Model Selection - using variants of common methods [7, 8].
- Flexibility - many choices to match model to data [2, 5].
- Transparency - model is formally specified.
- Efficiency - proper statistical inference [1, 7].

References


Example Species Archetypes from Fish Biomass Data

[Figure 1: Example results from a SAM analysis. Maps are for expected biomass, on the log scale.]

Example Regions of Common Profiles for Fish in North West Australia

[Figure 2: Example results from an RCP analysis. Maps are for the probability of each region type occurring at each location.]